

Unit 8 Solving Equations & Inequalities

8.6 Solving Single-Step Inequalities (text 9.2)

Consider the inequality $-3 < 6$. How do mathematical operations $[+, -, \times, \div]$ affect the inequality?

$$\begin{array}{llll}
 -3 < 6 & -3 < 6 & 6 \times -3 < 6 \times 6 & -3 < 6 \\
 +3 & +3 & -7 & -7 & -18 < 36 & \frac{-3}{3} < \frac{6}{3} \\
 0 < 9 & -10 < -1 & & -1 < 2 & \boxed{-3 - 3 < 6 - 3} & \boxed{\frac{-3}{-1} < \frac{6}{-1}}
 \end{array}$$

9 > -18 3 > -6 !

Conclusion: When we multiply or divide by a negative number the inequality reverses (flips).

Ex. Solve, show solution algebraically and graphically:

a) $x - 3 \geq 2$

$$x \geq 5$$



b) $-2x < 8$

$$x > -4$$



c) $3(-5) > \left(\frac{x}{8}\right)$

$$-15 > x \quad \text{OR} \quad x < -15$$



d) $4x \leq 10$

$$x \leq \frac{5}{2}$$



e) $\left(\frac{x}{8}\right) < (-24)(8)$

$$x > 192$$



f) $5 - x > 8$

$$-x = 3$$

$$x = -3$$

$$-x > 3$$

$$x < -3$$



Ex. A games store has a sale offering all games for \$12.50 each. If you only had \$80, how many games could you buy?

Let $g = \# \text{ games}$

money spend $\leq$ money have

$$12.5g \leq 80$$

$$g \leq 6.4$$

You can buy up to a max of 6 games