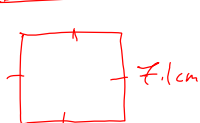


Unit 2: Working With Rational Numbers

2.4 Square Roots of Rationals

*Recall – to **square** a number is to multiply the number by itself (ie. exponent 2)

Ex. Estimate and calculate the area of a square with side lengths of 7.1 cm.



$$A = s^2$$

$$A = 7.1^2 = \boxed{50.41 \text{ cm}^2}$$

$$\approx 7^2 \approx 49 \text{ cm}^2$$

A **square root** is the inverse (opposite) operation.

Ex. A square has an area of 81 m^2 . What is the length of each side?



$$A = s^2$$

$$81 = s^2$$

$$s = \sqrt{81} = \boxed{9 \text{ m}}$$

Ex. Evaluate:

a) $\sqrt{9}$
 $= \boxed{3}$

b) $\sqrt{1}$
 $= \boxed{1}$

c) $\sqrt{576}$
 $= \boxed{24}$



Perfect Square: A number that can be expressed a product of two equal factors

Perfect Whole Number Squares: 1 4 9 16 25 36 49 64 81 100 121 144 169

Roots: 1 2 3 4 5 6 7 8 9 10 11 12 13

Ex. Which of the following are perfect rational squares? Determine the rational root if possible.

a) 169 ✓

$$\sqrt{169} = 13$$

b) $\frac{25}{49}$ ✓

$$\sqrt{\frac{25}{49}} = \frac{5}{7}$$

c) $\frac{2}{9}$ X

2 is not a perfect square

d) 0.4

$$\frac{4}{10} \text{ X}$$

e) $\frac{121}{64}$ ✓

$$\sqrt{\frac{121}{64}} = \frac{11}{8}$$

f) 12.1

$$\frac{121}{10} \text{ X}$$

g) 1.21

$$\frac{121}{100} \text{ ✓}$$

$$\sqrt{\frac{121}{100}} = \frac{11}{10} = 1.1$$

h) 0.121

$$\frac{121}{1000} \text{ X}$$

i) 0.0121

$$\sqrt{\frac{121}{10000}} = \frac{11}{100}$$

Ex. Evaluate with and without a calculator:

$$\begin{aligned} \text{a) } & \sqrt{1.44} \\ & \sqrt{\frac{144}{100}} \\ & = \frac{12}{10} \\ & = \boxed{1.2} \end{aligned}$$

$$\begin{aligned} \text{b) } & \sqrt{0.16} \\ & \sqrt{\frac{16}{100}} \\ & = \frac{4}{10} \\ & = \boxed{0.4} \end{aligned}$$

The roots of non-perfect squares can be estimated and verified with our calculator.

Ex. Estimate & calculate. 1 4 9 16 25 36 49 64 81 100

$$\begin{aligned} \text{a) } & \sqrt{11} \\ & \sqrt{9} \leftarrow \sqrt{11} \leftarrow \sqrt{16} \\ & 3 \leftarrow \leftarrow 4 \\ & \approx 3.2 \end{aligned}$$

$$\sqrt{11} = 3.32$$

$$\begin{aligned} \text{b) } & \sqrt{30} \\ & \sqrt{25} \leftarrow \sqrt{30} \leftarrow \sqrt{36} \\ & 5 \leftarrow \leftarrow 6 \\ & \approx 5.4 \end{aligned}$$

$$\sqrt{30} = 5.48$$

$$\begin{aligned} \text{c) } & \sqrt{0.73} \\ & \sqrt{0.64} \leftarrow \sqrt{0.73} \leftarrow \sqrt{0.81} \\ & 0.8 \leftarrow \leftarrow 0.9 \\ & \approx 0.85 \text{ or } 0.86 \end{aligned}$$

$$\sqrt{0.73} = 0.854$$

$$\begin{aligned} \text{d) } & \sqrt{0.34} \\ & \sqrt{0.25} \leftarrow \sqrt{0.34} \leftarrow \sqrt{0.36} \\ & 0.5 \leftarrow \leftarrow 0.6 \\ & \approx 0.58 \text{ or } 0.59 \end{aligned}$$

$$\sqrt{0.34} = 0.583$$