

Unit 8: Logarithmic Functions**8.4 Logarithms & Exponential Equations****Part I: Use logarithms to solve for exponents**

$$\text{If } L = R \text{ then } \log_c L = \log_c R$$

Ex. Solve to the nearest hundredth:

a) $2^x = 5$

b) $8(3^{2x}) = 568$

c) $3^{x+2} = 5^{2x-3}$

Ex. A city's population doubles every 8 years. How long, to the nearest year, will it take for the population to grow from 25,000 to 1 million people?

$$F = I r^{t/n}$$

Ex. Evaluate to the nearest hundredth:

$$\log_5 782$$

The previous example demonstrates the Change of Base Rule:

$\log_c a = \frac{\log_x a}{\log_x c}$
--

x is a base of your choosing

*also use to graph non base 10 logs with calc

Ex. Graph $\log_3(x - 1) + 2$ with your calculator & sketch below.

Ex. Evaluate to the nearest tenth:
 $\log_3 16$

Ex. Evaluate without a calculator:
 $\log_4 32$

Part II: Solving logarithmic equations

Case I Equations with all log terms **If $\log_c x = \log_c y$ then $x = y$**

Ex. Solve:

a) $\log_3(3x + 1) = \log_3 2 + \log_3 8$

b) $\log x = \log 4 - \log(x - 3)$

Case II Equations with log terms and constant terms

If $\log_c x = y$ then $c^y = x$

Ex. Solve:

a) $\log_8(x + 3) - 1 = -\log_8(x + 1)$

b) $\log_2(3 - x) + \log_2(1 - x) = 3$