

Unit 3: Quadratic Equations

3.1 Graphical Solutions of Quadratic Equations

Quadratic Equation: a 2nd degree equation with standard form
 $ax^2 + bx + c = 0$; $a \neq 0$

$$\text{ex. } \boxed{2x^2 + 12x + 16 = 0}$$

$$3x^2 = -2 + 5x$$

Root(s) of an equation:

- the solution(s) to an equation
- value(s) of the variable that satisfies the equation

Zero(s) of a function:

- the value(s) of $f(x)$ for which $f(x) = 0$
- the x -intercept(s) of the graph of $f(x)$

ex. Determine the roots of each equation by graphing by hand:

$$x^2 - 8x + 16 = 0$$

graph $f(x) = x^2 - 8x + 16$

$$= (x^2 - 8x + 16) + 16 - 16$$

$$f(x) = (x - 4)^2$$

vertex (4, 0)

The zero(s) are
the roots of
the equation.

$$\boxed{x = 4}$$

$$-2x^2 = 8x$$

$$-2x^2 - 8x = 0$$

$$\text{OR } 0 = 2x^2 + 8x$$

$$f(x) = 2(x^2 + 4x + 4) - 8$$

$$= 2(x + 2)^2 - 8$$

$$\boxed{x = 0, -4}$$

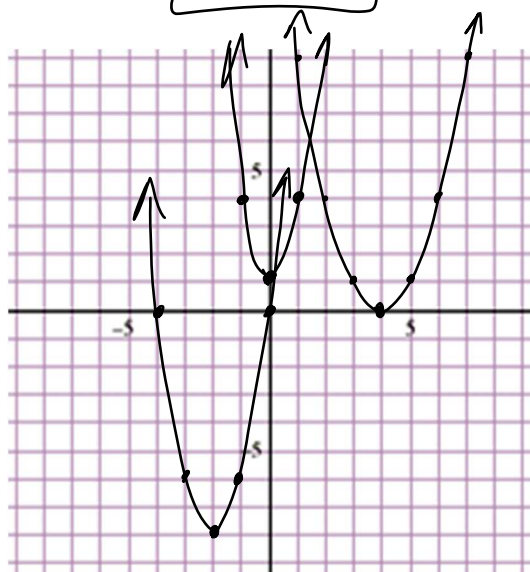
$$3x^2 = -1$$

$$3x^2 + 1 = 0$$

$$f(x) = 3x^2 + 1$$

no zeros

$\therefore$ $\boxed{\text{no roots}}$



Check:

$$x^2 - 8x + 16 = 0$$

$$(4)^2 - 8(4) + 16$$

$$16 - 32 + 16$$

$$0 = 0 \checkmark$$

$$-2x^2 = 8x$$

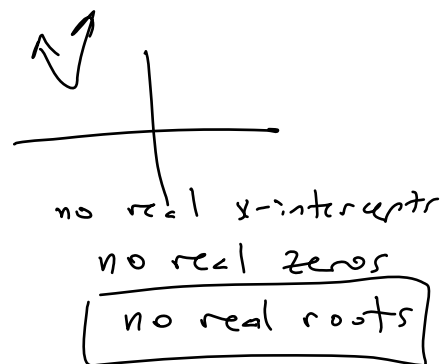
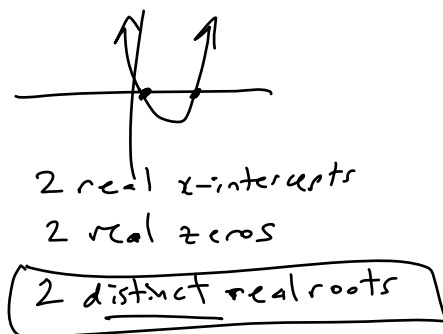
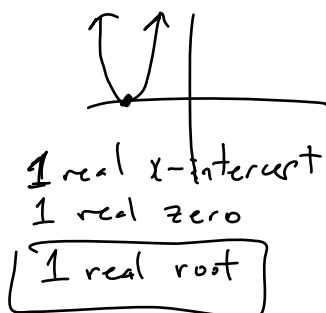
$$-2(0)^2 = 8(0)$$

$$0 = 0 \checkmark$$

$$-2(-4)^2 = 8(-4)$$

$$-32 = -32 \checkmark$$

Possible number of solutions to a quadratic equation:

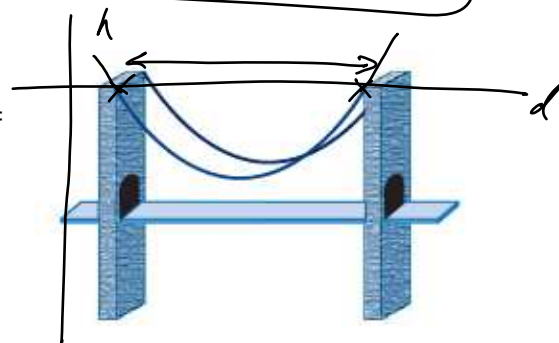


ex. The manager of Jasmine's Fine Fashions is investigating the effect that raising or lowering dress prices has on the daily revenue from dress sales. The function $R(x) = 100 + 15x - x^2$ gives the store's revenue R , in dollars, from dress sales, where x is the price change, in dollars. What price changes will result in no revenue?

$$\begin{aligned} R(x) &= 0 \\ 100 + 15x - x^2 &= 0 \\ x &= 20 \text{ \& } x = -5 \end{aligned}$$

A decrease in price of \$5 or an increase in price of \$20 will result in no revenue.

ex. The curve of a suspension bridge cable attached between the tops of two towers can be modeled by the function $h(d) = 0.0025(d - 100)^2 - 10$, where h is the vertical distance from the top of a tower to the cable and d is the horizontal distance from the left end of the bridge, both in meters. What is the horizontal distance between the two towers? Express your answer to the nearest tenth of a meter.



$$\begin{aligned} h(d) &= 0 \\ 0.0025(d - 100)^2 - 10 &= 0 \\ d &= 36.75 \text{ \& } d = 163.25 \\ 163.25 - 36.75 &= 126.5 \text{ m} \end{aligned}$$