

Write the equation of the line with the given characteristics. Answers in the form(s) requested.

1. Slope -3 and y-intercept 4. [slope-intercept & general form]

$$\boxed{y = -3x + 4} \quad \boxed{3x + y - 4 = 0}$$

2. Slope $\frac{2}{3}$ and point $(-6, 1)$. [slope-point & slope-intercept form]

$$\boxed{y - 1 = \frac{2}{3}(x + 6)} \quad y - 1 = \frac{2}{3}x + 4$$

$$\boxed{y = \frac{2}{3}x + 5}$$

3. Points $(6, -4)$ and $(0, 4)$. [slope-point & general form]
 $b = 4!$

$$m = \frac{-4 - 4}{6 - 0}$$

$$= \frac{-8}{6}$$

$$= -\frac{4}{3}$$

$$\boxed{y + 4 = -\frac{4}{3}(x - 6)}$$

$$\boxed{y - 4 = -\frac{4}{3}(x - 0)}$$

$$\begin{aligned} & \text{Multiply by 3} \\ & 3(y - 4) = -4(x - 0) \\ & 3y - 12 = -4x \\ & \boxed{4x + 3y - 12 = 0} \end{aligned}$$

4. Slope $-\frac{3}{2}$ and x-intercept 3. [slope-intercept form]
 $(3, 0)$

$$y = -\frac{3}{2}x + b$$

$$0 = -\frac{3}{2}(3) + b$$

$$0 = -\frac{9}{2} + b$$

$$\frac{9}{2} = b$$

$$\boxed{y = -\frac{3}{2}x + \frac{9}{2}}$$

$$\begin{aligned} & \text{or} \\ & y - 0 = -\frac{3}{2}(x - 3) \\ & \boxed{y = -\frac{3}{2}x + \frac{9}{2}} \end{aligned}$$

5. X-intercept -4 and y-intercept 5. [slope-point form]

$$(-4, 0)$$

$$(0, 5)$$

$$m = \frac{5 - 0}{0 - (-4)}$$

$$m = \frac{5}{4}$$

$$\boxed{y - 0 = \frac{5}{4}(x + 4)}$$

$$\text{or} \quad \boxed{y - 5 = \frac{5}{4}(x - 0)}$$

6. Parallel to $x - 3 = 0$ and point $(-2, 5)$. [general form]

same
slope

vertical

slope = undefined

$$x = -2$$

$$\boxed{x + 2 = 0}$$

$$m_{\parallel} = \text{undefined}$$

7. Perpendicular to $x + 5 = 0$ and point $(3, 4)$ [general form]

negative
reciprocal

slope

vertical
 $m = \text{undefined}$

$\therefore m_{\perp} = 0$ horizontal line

$$y = 4$$

$$\boxed{y - 4 = 0}$$

8. Parallel to $y = -2x + 4$ and same y-intercept as $y = x - 3$ [slope-intercept form]

same
slope

$$m = -2$$

$$\therefore m_{\parallel} = -2$$

$$b = -3$$

$$\boxed{y = -2x - 3}$$

9. Perpendicular to $3x + 2y = 6$ and point $(3, -4)$ [slope-point form]

$$2y = -3x + 6$$

$$y = -\frac{3}{2}x + 3$$

$$m = -\frac{3}{2}$$

$$\therefore m_{\perp} = \frac{2}{3}$$

$$\boxed{y + 4 = \frac{2}{3}(x - 3)}$$

10. Parallel to $x - 3y + 6 = 0$ with the same x-intercept as $y = 2x + 8$ [general form]

$$x + y = 0$$

$$3y = x + 6$$

$$y = \frac{1}{3}x + 2$$

$$m = \frac{1}{3}$$

$$m_{\parallel} = \frac{1}{3}$$

$$y - 0 = \frac{1}{3}(x + 4)$$

$$3(y) = (\frac{1}{3}x + \frac{4}{3}) \cdot 3$$

$$3y = x + 4$$

$$0 = 2x + 8$$

$$-8 = 2x$$

$$-4 = x - 2 \quad \text{Point } (-4, 0)$$

$$\rightarrow \boxed{x - 3y + 4 = 0}$$

11. Perpendicular to $3x = 4y + 12$ with the same y-intercept as $y + 3 = 2x$ [all forms]

$$4y = 3x - 12$$

$$y = \frac{3}{4}x - 3$$

$$m = \frac{3}{4}$$

$$\therefore m_{\perp} = -\frac{4}{3}$$

$$\boxed{y = -\frac{4}{3}x - 3}$$

$$y = 2x - 3$$

$$\text{y-intercept } (0, -3)$$

$$\frac{1}{3}(y) = (-\frac{4}{3}x - 3) \cdot \frac{1}{3}$$

$$3y = -4x - 9$$

$$\boxed{y + 3 = -\frac{4}{3}(x - 0)}$$

$$\boxed{4x + 3y + 9 = 0}$$