

Factor each expression:

1. $8m^3 - 4m^2$

$$4m^2(2m-1)$$

2. $30x^2y - 20x^2y^2 + 10x^3y^2$

$$10x^2y(3-2y+xy)$$

3. $2ax - ay + 4bx - 2by$

$$a(2x-y) + 2b(2x-y)$$

$$(2x-y)(a+2b)$$

4. $6x^2 + 2xy - 15x - 5y$

$$2x(3x+y) - 5(3x+y)$$

$$(3x+y)(2x-5)$$

5. $2x^2 + 7x + 5$

$$\begin{array}{r} 2x^2 + 2x + 5x + 5 \\ \hline 2x(x+1) + 5(x+1) \\ \hline (x+1)(2x+5) \end{array}$$

6. $6x^2 - 11xy + 3y^2$

$$\begin{array}{r} 6x^2 - 2xy - 9xy + 3y^2 \\ \hline 2x(3x-y) - 3y(3x-y) \\ \hline (3x-y)(2x-3y) \end{array}$$

7. $a^2 + 5a - 14$

$$\begin{array}{r} (a+7)(a-2) \\ \hline \end{array}$$

8. $p^2 - 5pq - 24q^2$

$$\begin{array}{r} (p-8q)(p+3q) \\ \hline \end{array}$$

Completely factor each expression:

9. $12a^3 - 94a^2 - 16a$

$$\begin{array}{l} 2a(6a^2 - 47a - 8) \\ \begin{array}{r} \times -48 \\ + -47 \\ \hline -48, 1 \end{array} \\ \downarrow \\ \begin{array}{r} 6a^2 - 48a + a - 8 \\ 6a(a-8) + 1(a-8) \end{array} \\ \downarrow \\ \boxed{2a(a-8)(6a+1)} \end{array}$$

11. $6m^2n - 12mn^2 - 10mn + 20n^2$

$$\begin{array}{l} 2n(3m^2 - 6mn - 5m + 10n) \\ \downarrow \\ 3m(m-2n) - 5(m-2n) \\ \downarrow \\ \boxed{2n(m-2n)(3m-5)} \end{array}$$

10. $7c^2d - 35cd^2 + 42d^3$

$$\begin{array}{l} 7d(c^2 - 5cd + 6d^2) \\ \begin{array}{r} \times 6 \\ + -5 \\ \hline -2, -3 \end{array} \\ \downarrow \\ \boxed{7d(c-2d)(c-3d)} \end{array}$$

Determine ALL integral values of k so that each trinomial can be factored:

12. $x^2 + kx - 9$

$$\begin{array}{c|c} \times -9 & + k \\ \hline -1 & 9 \rightarrow 8 \\ 1 & -9 \rightarrow -8 \\ -3 & 3 \rightarrow 0 \end{array} \quad \boxed{k = 0, \pm 8}$$

13. $3x^2 + kx + 7$

$$\begin{array}{c|c} \times 21 & + k \\ \hline 1 & 21 \rightarrow 22 \\ -1 & -21 \rightarrow -22 \\ 3 & 7 \rightarrow 10 \\ -3 & -7 \rightarrow -10 \end{array} \quad \boxed{k = \pm 10, \pm 22}$$

Determine TWO integral values of k so that each trinomial can be factored:

14. $x^2 - 3x + k$

$$\begin{array}{c|c} \times k & + -3 \\ \hline 2 & -1 \rightarrow -2 \\ -4 & -4 \rightarrow +1 \\ -10 & -5 \rightarrow +2 \end{array} \quad \boxed{k = 2, -4, -10, \dots}$$

15. $3x^2 + 4x + k$

$$\begin{array}{c|c} \times 3k & + 4 \\ \hline 3 & 1 \rightarrow 3 \\ -12 & 6 \rightarrow -2 \\ -45 & 9 \rightarrow -5 \end{array} \quad \begin{array}{l} 3k = 3 \quad 3k = -12 \quad 3k = -45 \\ k = 1 \quad k = -4 \quad k = -9 \end{array}$$