

Date: _____

Unit 5: Linear Equations & Graphs**5.0 Slope**

Slope: The ratio of the vertical change (rise) to the horizontal change (run) of a line or a line segment.

Average rate of change.

$$\text{slope} = \frac{\text{vertical change}}{\text{horizontal change}}$$

$$\text{or } m = \frac{\text{rise}}{\text{run}}$$

$$\text{or } m = \frac{\Delta y}{\Delta x}$$

* Δ = delta
"change in"

A positive change in both the vertical and horizontal values leads to a

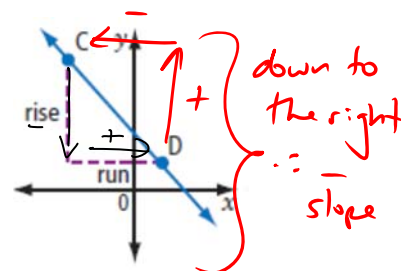
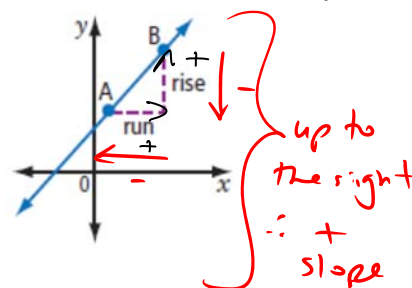
positive slope.

A negative change in both the vertical and horizontal values leads to a

positive slope.

A negative change in one and a positive change in the other leads to a

negative slope.



Ex. Classify the slope of each line segment as positive, negative or neither. Then, calculate each slope. $m = \text{slope}$

$$m_{AB} = \frac{7}{5}$$

$$m_{CD} = \frac{10}{0}$$

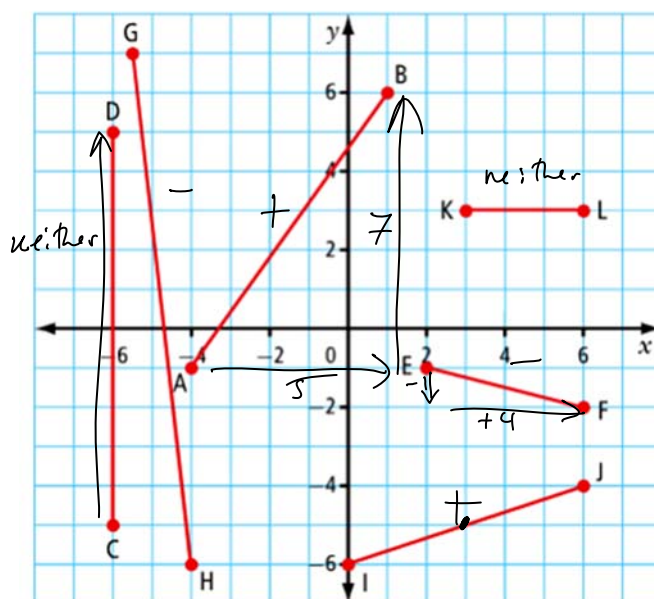
= undefined ← for all vertical lines

$$m_{EF} = \frac{-1}{4}$$

$$m_{IJ} = \frac{2}{6} = \frac{1}{3}$$

$$m_{GH} = \frac{-13}{1.5} \times 2 = \frac{-26}{3}$$

$$m_{KL} = \frac{0}{3} = 0$$



Slope formula: Given two points (x_1, y_1) and (x_2, y_2) the slope between them is $m = \frac{y_2 - y_1}{x_2 - x_1}$ * on data sheet

Ex. What is the slope, m , of each line segment with the given endpoints?

a) $S(-3, 6)$ and $T(5, 2)$
 x_1, y_1 x_2, y_2

$$m = \frac{2 - 6}{5 - (-3)} \quad \text{or} \quad \frac{6 - 2}{-3 - 5}$$

$$= \frac{-4}{8} \quad = \frac{4}{-8}$$

$$= -\frac{1}{2} \quad = -\frac{1}{2}$$

b) $H(4, 3)$ and $K(4, 8)$

$$m = \frac{3 - 8}{4 - 4}$$

$$= \frac{-5}{0}$$

$$m = \text{undefined}$$

c) $M(-9, -7)$ and $N(-1, -7)$

$$m = \frac{-7 - (-7)}{-1 - (-9)}$$

$$= \frac{0}{8} = \rightarrow m = 0$$

↑ ↑
horizontal line

Ex. The point $(-3, 2)$ is on a line that has a slope of $\frac{-3}{4}$. List three other points on the line.

$(-3, 2)$
 $+4 \quad -3$

$(1, -1)$ or $(-3, 2)$
 $+4 \quad -3$ $-4 \quad +3$

$(5, -4)$ $(-7, 5)$

$\frac{-3}{4} \leftarrow \text{rise} \rightarrow \frac{-3}{4}$
 $\frac{-3}{4} \leftarrow \text{run} \rightarrow -4$

Ex. The point $(-6, 1)$ is on a line that has a slope of $\frac{1}{3}$. List three other points on the line.

$(-9, 0)$
 $-3 \quad -1$

$(-6, 1)$

$= \frac{1}{3}$

Ex. Graph the line with given point and slope:

a) $(-3, 2), m = -\frac{1}{3}$

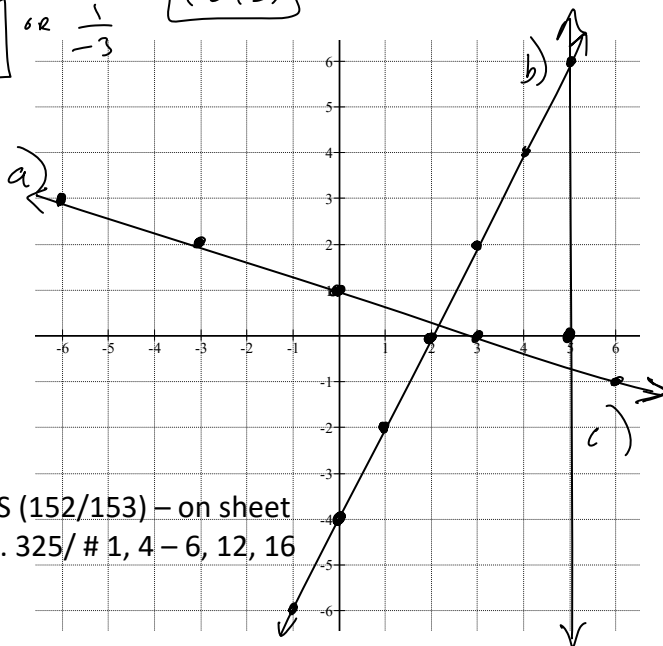
$-\frac{1}{3}$ or $\frac{1}{-3}$

b) $(0, -4), m = 2$

$(0, 3)$

c) $(5, 0), m = \text{undefined}$

* at least 3 points



Practice:

WS (152/153) – on sheet
 pg. 325/ # 1, 4 – 6, 12, 16