

Date: _____

4.2 Linear Relations

Relation:

- an association between two quantities
- a rule that turns input values into output values

A relation can be presented in a variety of ways. For example,

Words

Three times the length of your ear, e , is equal to the length of your face, f , (from chin to hairline).

Equation

$$f = 3e$$

$\uparrow$ output $\uparrow$ input

Ordered Pairs (points)

(e, f) (x, y)

ex. $(2.5 \text{ cm}, 7.5 \text{ cm})$ $(4 \text{ cm}, 12 \text{ cm})$ $(1 \text{ cm}, 3 \text{ cm})$

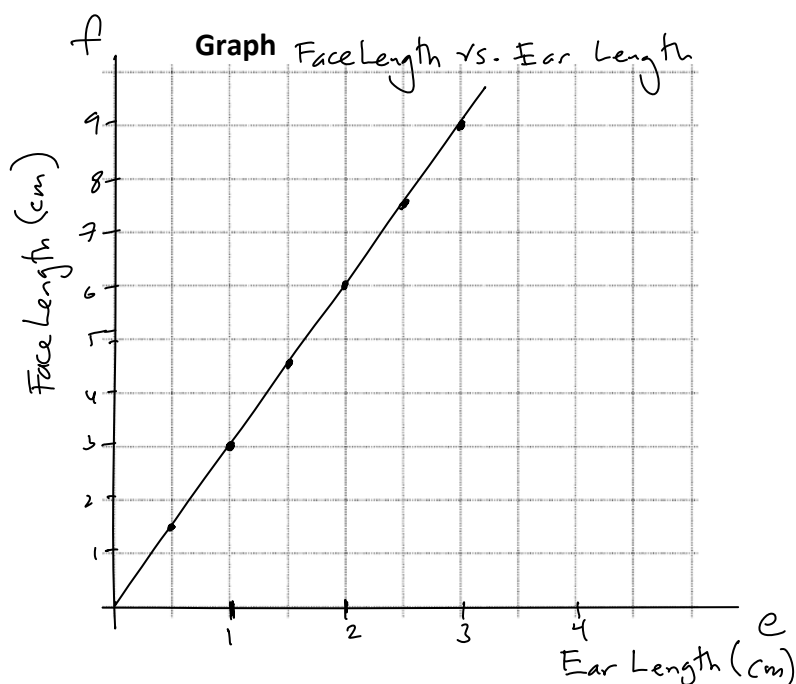
$\uparrow$ input $\uparrow$ output

Table of Values

Ear Length, e (cm)	Face Length, f (cm)
0.5	1.5
1	3
1.5	4.5
2	6
2.5	7.5
3	9

$\uparrow$
independent

$\uparrow$
dependent

**Independent Variable:**

- The input variable
- Graphed on x-axis
- ex. ear length

Dependent Variable:

- The output variable
- Graphed on y-axis
- ex. face length

Linear Relation:

- forms straight line when graphed
- values of y are inc/dec by a constant as x inc/dec by some constant
- 1 or 2 variable equation of degree 1

Ex. Table of Values

Linear

x	y
2	17
3	14
4	11
5	8

$\downarrow +1$ $\downarrow -3$

Non-linear Relation:

* does not form a straight line

Non-Linear

x	y
0	1
2	3
4	6
6	10

$\downarrow +2$ $\downarrow +3$ $\downarrow +4$

Ex. Equations

Linear

$$\left. \begin{array}{l} x = 7 \\ 3m + 2n = -12 \\ y = -\frac{2}{3}x + 5 \\ y = -3 \end{array} \right\} \text{degree 1}$$

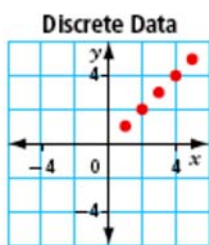
Non-Linear

$$\begin{array}{l} 2x + y^2 = 6 \\ h = k^3 \\ xy = 3 \\ y = \frac{1}{x} \end{array}$$

Discrete Data:

Values are not connected

For data that cannot have values between

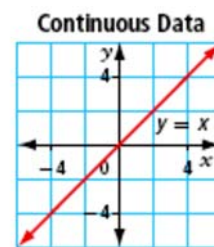


ex. selling muffins for \$1 each

Continuous Data:

Values are connected

Has infinite divisions between whole value points.



Ex. In a frog jumping championship there is a frog named George who jumps a distance of 2m in a single leap. George maintains a distance of 2m every jump; the total distance travelled is measured after every jump. Consider the relationship between the number of jumps and the total distance travelled.

- a) Create a variable to represent each quantity in the relation. Which is the dependent variable? Which is the independent variable?

Let $j = \# \text{ of jumps} \leftarrow \text{independent}$
 $d = \text{total distance} \leftarrow \text{dependent}$

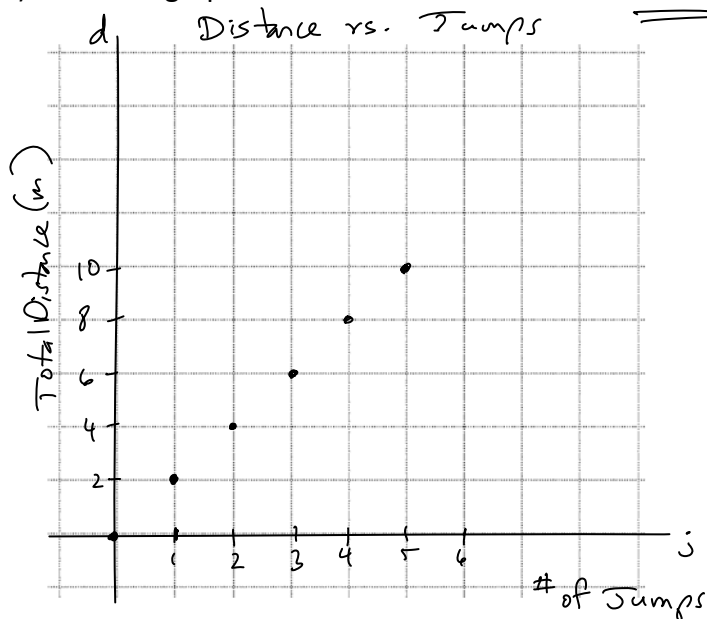
- b) Create a table of values for this relation. What are appropriate values for the independent variable?

$j(\#)$	$d(m)$
0	0
1	2
2	4
3	6
4	8
5	10

- c) Identify the relationship as linear or non-linear. Explain how you know.

Linear, distance increases by a constant +2m as the # of jumps increases by a constant +1.

- d) Create a graph for the relation. Are the data discrete or continuous?



Discrete - no
partial
 jumps