

Date: _____

Unit 2: Exponents & Roots

2.1 – Factor Trees, GCF, & LCM

Prime Numbers: Numbers with only two distinct factors of 1 and itself.

Ex. 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, ...
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 only even prime!

Composite Numbers: Numbers with more than two factors.

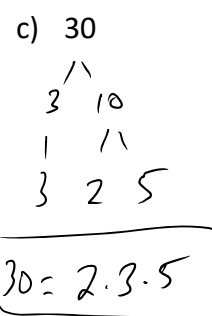
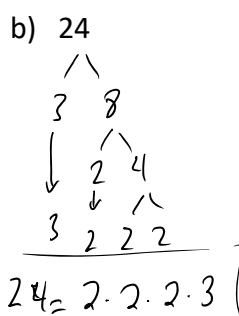
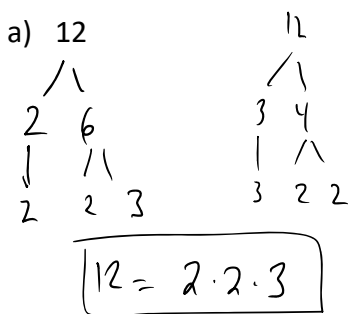
Ex. 4, 6, 8, 9, 10, 12, 14, 15, 16, ...

Prime Factorization: Expressing a composite number as a product of prime factors.

Ex. $10 = 2 \cdot 5$ $8 = 2 \cdot 2 \cdot 2$

A factor tree is useful to prime factor a number.

Ex. Use a factor tree to find the prime factorization of each given number:



Greatest Common Factor (GCF): The largest common factor among a group of two or more numbers.

Ex. Use prime factorization to identify the GCF in each group of numbers:

a) 12 and 24

$$12 = 2 \cdot 2 \cdot 3$$

$$24 = 2 \cdot 2 \cdot 2 \cdot 3$$

GCF = multiply the common factors together

$$= 2 \cdot 2 \cdot 3$$

$GCF = 12$

b) 24 and 30

$$24 = 2 \cdot 2 \cdot 2 \cdot 3$$

$$30 = 2 \cdot 3 \cdot 5$$

$$GCF = 2 \cdot 3$$

$GCF = 6$

c) 12, 24, and 30

$$12 = 2 \cdot 2 \cdot 3$$

$$24 = 2 \cdot 2 \cdot 2 \cdot 3$$

$$30 = 2 \cdot 3 \cdot 5$$

$$GCF = 2 \cdot 3$$

$GCF = 6$

Ex. Multiples of 5: 5, 10, 15, 20, 25, ...

Least Common Multiple (LCM): The smallest common multiple among a group of two or more numbers.

Ex. Use prime factorization to identify the LCM in each group of numbers:

a) 12 and 24

$$\begin{aligned} 12 &= 2 \cdot 2 \cdot 3 \\ 24 &= 2 \cdot 2 \cdot 2 \cdot 3 \end{aligned}$$

LCM = multiply all factors
BUT only once for
any common factor

$$= 2 \cdot 2 \cdot 2 \cdot 3$$

$LCM = 24$

b) 24 and 30

$$\begin{aligned} 24 &= 2 \cdot 2 \cdot 2 \cdot 3 \\ 30 &= 2 \cdot 3 \cdot 5 \end{aligned}$$
$$LCM = 2 \cdot 2 \cdot 2 \cdot 3 \cdot 5$$

$LCM = 120$

c) 12, 24, and 30

$$\begin{aligned} 12 &= 2 \cdot 2 \cdot 3 \\ 24 &= 2 \cdot 2 \cdot 2 \cdot 3 \\ 30 &= 2 \cdot 3 \cdot 5 \end{aligned}$$
$$LCM = 2 \cdot 2 \cdot 2 \cdot 3 \cdot 5$$

$LCM = 120$